



統計科學研究所

INSTITUTE OF  
STATISTICAL SCIENCE



S.E.M.I.N.A.R.

S.T.A.T.I.S.T.I.C.S.

## Seminar

Title : The genus distribution of cubic graphs and asymptotic number of rooted cubic maps with high genus

Speaker : Prof. Jason (Zhicheng) Gao ( 高志成 教授 )  
( School of Mathematics and Statistics, Carleton University, Canada)

Time : 10:30 AM~12:00 PM, Tuesday, Dec 6, 2022

Place : Room308 , Institute of Statistical Science

## Abstract

Let  $C_{\{n,g\}}$  be the number of rooted cubic maps with  $2n$  vertices on the orientable surface of genus  $g$ . We show that the sequence  $(C_{\{n,g\}} : g \geq 0)$  is asymptotically normal with mean and variance asymptotic to  $(1/2)(n - \ln n)$  and  $(1/4) \ln n$ , respectively. We derive an asymptotic expression for  $C_{\{n,g\}}$  when  $(n - 2g)/\ln n$  lies in any closed subinterval of  $(0, 1)$ . Using rotation systems and Bender's theorem about generating functions with fast-growing coefficients, we derive simple asymptotic expressions for the numbers of rooted regular maps, disregarding the genus.

In particular, we show that the number of rooted cubic maps with  $2n$  vertices, disregarding the genus, is asymptotic to  $(3/\pi)n! 6^n$ .

※ Online live streaming through Cisco Webex will be available.

※ The tea reception will be held at 10:10.